Pervaporation, Solubility Aspects of the Solution-Diffusion Model

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PERVAPORATION, SOLUBILITY ASPECTS OF THE
SOLUTION-DIFFUSION MODEL

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INTRODUCTION.

Pervaporation is a membrane process where a liquid mixture is in
direct contact at one side of the membrane, the upstream side and
the permeated product is removed as a vapour at the downstream
side by applying a low partial pressure. This can be achieved
either by creating a vacuum or by using a carrier gas (fig. 1).
Pervaporation is the only membrane process where a phase transi-
tion occurs going from upstream side to downstream side.
The commercialization of the pervaporation process is under-devel-
oped compared to other membrane processes such as microfiltration,
ultrafiltration or hyperfiltration. Around the sixties Binning and
coworkers tried to introduce pervaporation as an industrial pro-
cess but their attempts were not very successful despite intensive
investigations and a number of patents [1]. The main reason for
this failure was undoubtedly that permeation rate and/or selecti-
vity were insufficient for commercial application.
Other reasons for a long incubation time of this process are:
  energy consumption is relatively high compared to other membrane

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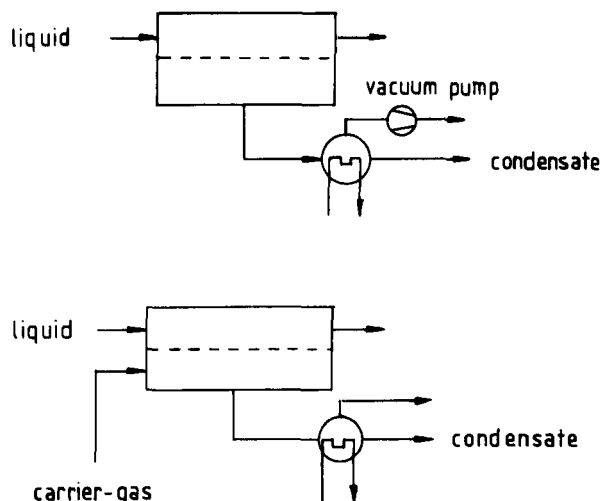
FIGURE 1. PERVAPORATION WITH DOWNSTREAM VACUUM OR A CARRIER-GAS.

processes such as microfiltration, ultrafiltration or hyperfil-
tration because a phase transition occurs and the heat
of vaporization has to be supplied.
- process design is difficult because of a temperature drop across
the membrane and pressure losses at the downstream side.

In the last decade there has been a renewed interest in pervapora-
tion especially in the field of ethanol-water separation. The
attractiveness of this specific application is the need to produce
fuels from renewable resources. Ethanol can be obtained by fermen-
tation of biomass. **Dehydration** of ethanol can be completely or
partly accomplished by pervaporation. Except for the alcohol-water
separation there are a number of other potential applications.
Pervaporation will especially be **competitive with other separation**
techniques when the concentration of the component which has to be
removed is low. Therefore the major field of application will be:

- dehydration of organic liquids containing small amounts of water
  (<20%).
- removal of organic contaminants such as aromatics and chlorinat-
  ed hydrocarbons from waste water.
- separation of azeotropic mixtures where the azeotropic composi-
  tion is not too far from one of the pure components (examples
  are: water/ethanol; water/i-propanol; water/t-butanol; water/-
  THF; water/dioxane; methanol/acetone; ethanol/hexane; propanol/-
  cyclohexane; etc.).

The selectivity towards a liquid mixture is expressed by the se-
lectivity factor α.

$$\alpha_{A/B} = \frac{X_A/X_B}{Y_A/Y_B} \qquad [1]$$

where X_A and X_B are the concentrations of components A and B in
the permeate and Y_A and Y_B are the concentrations in the liquid
feed. The pervaporation process essentially involves a sequence of
three steps:
. selective sorption into the membrane
. selective diffusion through the membrane
. desorption into a vapour phase at the downstream side.

Transport through a pervaporation membrane takes place by a solu-
tion-diffusion mechanism [2-5], i.e. the permeation rate is a
function of solubility and diffusivity. Solubility is a thermody-
namic property and diffusivity is a kinetic property and both
affect selectivity. When two or more components are permeating
through a membrane coupling will occur in general. This means that
in the case of a binary mixture the flux of a component in the
membrane is not only determined by the presence of the other com-
ponent but also by its movement, i.e. coupling takes place in the
solubility part as well as in the diffusivity part according to

$$J_i = f\left[S_i(c_i,c_j),D_i(c_i,c_j)\right] \qquad [1]$$

S_i is the solubility of component i and D_i its diffusivity.
Many investigators made use of concentration dependent diffusion
coefficients depending on the concentrations of all the components
present but generally coupling in the solubility part was neglect-
ed. In most cases ideal sorption was assumed [6-8], i.e. the con-
centration of a component in the membrane was supposed to be di-
rectly proportional to the concentration of that component in the
liquid mixture. There is much experimental evidence that in gene-
ral ideal sorption does not occur [9-13]. Mostly one of the compo-
nents will be sorbed preferentially, i.e. preferential or selec-
tive sorption occurs. This means that the composition of the
liquid feed mixture inside the membrane is different from the
composition in the liquid feed mixture in such a way that there is
no linear relation between composition in the membrane and
composition in the feed.
The objective of this paper is to discuss the solubility part of
the solution-diffusion model in relation to selective transport.
Two different types of mixtures have been investigated: a weakly
interacting ('ideal') mixture, o-xylene/p-xylene and a strongly
non-ideal mixture, ethanol/water.
In the first part the fundamental aspects of polymer-penetrant
affinity will be described. The influence of preferential sorption
on selective transport will be discussed in the second part.

THEORY.

There are several solution theories which can describe the
solubility of low molecular weight substances in polymers. Two
widely used theories are i) the solubility parameter theory [14]
and ii) the Flory-Huggins theory [15]. There are also more
sophisticated solution theories such as the 'new' Flory theory
(derived from equation-of-state relations) [16] or the
fluid-lattice theory [17] which can describe polymer solution

thermodynamics more properly from a chemical-phyiscal point of view. However, there are still problems to describe the solubility behaviour quantitatively i.e. these new theories do not predict polymer-solution behaviour significantly better [18-20]. Furthermore these theories require physical and chemical data which are only available for a limited number of compounds. For describing polymer-penetrant affinity we will make use of the solubility parameter theory and of the Flory-Huggins theory.

Solubility parameter theory.

The solubility parameter theory is based on the concept of regular solutions. These are solutions having an ideal entropy of mixing and a non-ideal enthalpy of mixing.
In liquids there exist strong attractive forces between molecules and the potential energy of the molecules (relative to the molecules in the vapour phase) is called the cohesive energy. The intermolecular forces contributing to the cohesive energy can be divided into i) nonpolar interactions (dispersion or London forces), ii) polar interactions and iii) specific chemical forces such as hydrogen bonding. The cohesive energy density (CED) is defined as the ratio between cohesive energy (-E) and molar volume (V_m).

$$CED = {}^{-E}/V_m \qquad\qquad [3]$$

The cohesive energy is assumed to be equal to the total energy of vapourization. The solubility parameter (δ) is directly related to the cohesive energy density.

$$CED \equiv \delta^2 = \frac{\Delta E_{vap}}{V_m} \qquad\qquad [4]$$

Hansen [21] assumed that the total energy of vapourization is the sum of energies required to overcome dispersion forces (ΔE_d), and polar interactions (ΔE_p) and to break hydrogen bonds (ΔE_h).

$$\Delta E_{vap} = \Delta E_d + \Delta E_p + \Delta E_h \qquad [5]$$

Combining eqns. [4] and [5] gives

$$\delta^2 = \delta_d^2 + \delta_p^2 + \delta_h^2 \qquad [6]$$

A good solvent for a certain polymer will have a solubility parameter value close to that of the polymer.
The three-component solubility parameter can be considered as a vector lying in ($\delta_d, \delta_p, \delta_h$)-space. Each solvent and each polymer can be located in this ($\delta_d, \delta_p, \delta_h$)-space being the end-point of the radius vector (see fig. 2).
Consider a given polymer (subscript p) and a penetrant (subscript s, this can be a solvent or a nonsolvent), then the distance Δ between the end-points of the radius-vectors is given by [22, 23],

$$\Delta = \left[(\delta_{p,s} - \delta_{p,p})^2 + (\delta_{d,s} - \delta_{d,p})^2 + (\delta_{h,s} - \delta_{h,p})^2 \right]^{1/2} \qquad [7]$$

A schematical representation is given in fig. 2. Δ is a measure for the affinity between polymer and penetrant. When Δ decreases the affinity between polymer and penetrant will increase. When Δ approaches zero then the penetrant will be a solvent for the polymer. Table 1 gives the three-dimensional solubility parameters of
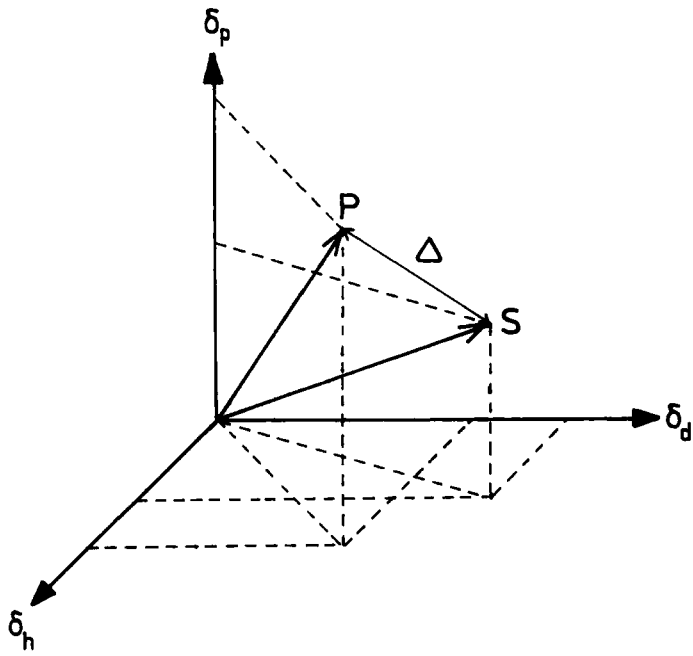
FIGURE 2.   SCHEMATIC REPRESENTATION OF POLYMER (P) AND SOLVENT (S)
             VECTORS IN $(\delta_p, \delta_d, \delta_h)$ SPACE; Δ IS THE DISTANCE BETWEEN
             END-POINTS OF VECTORS;

TABLE I [24]

	δ_d	δ_p	δ_h	δ
o-xylene	8.8	0.7	1.4	9.0
p-xylene	8.7	0	1.3	8.8
cellulose tripropionate	8.4	3.1	5.3	10.3

TABLE II [24]

binary system	Δ
cellulose tripropionate/o-xylene	4.4
cellulose tripropionate/p-xylene	4.9

the components of one of the systems discussed in this paper, o-xylene/p-xylene/cellulose tripropionate. The calculated values of the distance parameter Δ are given in table 2.

From table 2 it can be seen that the affinity of o-xylene to CTP is larger (the trend is small but significant) than the affinity of p-xylene to CTP. This is due to the presence of a dipole moment in o-xylene, whereas p-xylene has no dipole moment (see δ_p values in table 1).

There are some restrictions in using the solubility parameter theory. This theory accounts only for energetic contributions to the mixing process, entropic effects are disregarded. Furthermore, mixing of polymer and solvent is predicted from properties of the pure components so specific interactions between polymer and solvent occurring on mixing are not involved. At last, the theory can only be used for rather hydrophobic components and not for typically hydrophilic components, such as water and alcohols, having a high polar character or showing strong specific interactions such as hydrogen bonding. Therefore the solubility parameter approach can be used in a qualitative way only to a limited number of systems. For instance values for preferential sorption cannot be deduced from this theory as we will show later on. Nevertheless this theory is convenient to use and helpful as a first estimate of interaction phenomena. For more hydrophilic components such as water and alcohols the Flory-Huggins theory can be used.

Flory-Huggins theory [15].

In order to calculate the entropy of mixing of solvents and polym-
er (long-chain) molecules Flory and Huggins used a lattice model
where the segments of the polymer and the solvent molecules occupy
single sites.
For a binary system consisting of polymer and solvent the Gibbs
free enthalpy of mixing is given by

$$\Delta G_m = x_1 \ln v_1 + x_2 \ln v_2 + \chi_{12} x_1 v_2 \qquad [8]$$

where x and v are mole fraction and volume fraction respectively.
The first two terms on the right-hand side of eqn. 8 give the
ideal entropy of mixing while the last term describes the enthalpy
of mixing. This last term contains a binary interaction parameter
(the χ parameter) called the Flory-Huggins interaction parameter.
This parameter can be considered as a free energy parameter (in-
cluding both energetic and entropic contributions). It is a dimen-
sionless quantity characterizing the difference in interaction
energy of a solvent molecule immersed in pure polymer with respect
to the energy of a molecule immersed in pure solvent. For solvents
χ will have a value less than 0.5. When the affinity between poly-
mer and penetrant decreases χ will increase. The binary interac-
tion parameter of polymer and nonsolvent can be obtained from
swelling or sorption measurements [11]. For the systems water/-
ethanol/cellulose acetate and water/ethanol/polyacrylonitrile the
binary interaction parameters are given in table 3.
From table 3 it can be seen that the affinities of ethanol and
water to cellulose acetate are of the same order of magnitude with
ethanol having the highest affinity. Compared to cellulose acetate
polyacrylonitrile shows a different behaviour to water and etha-
nol. The affinity of ethanol to polyacrylonitrile is very small
while the affinity of water to the same polymer is much higher.

Sorption experiments.

The overall sorption values of ethanol-water mixtures in cellulose
acetate (CA), polyacrylonitrile (PAN) and polysulfone (PSf) are

TABLE III [11]

polymer	penetrant	χ
cellulose acetate	water	1.4
cellulose acetate	ethanol	1.1
polyacrylonitrile	water	1.8
polyacrylonitrile	ethanol	4.2

given in fig. 3. This figure clearly demonstrate the difference in
thermodynamic behaviour of the three polymers to ethanol-water
mixtures. Low swelling values can be observed for polyacryloni-
trile and polysulfone while cellulose acetate shows much higher
values. Polysulfone and polyacrylonitrile show an opposite be-
haviour, hardly any water sorption can be observed for polysulfone
while polyacrylonitrile shows a low value for pure ethanol. The
solubility of ethanol-water mixtures in cellulose acetate passes
through a maximum at about 65 weight % of ethanol in the feed.
Fig. 5 gives no information about the ethanol-water composition in
the membrane i.e. the occurence of preferential sorption cannot be
deduced from the overall sorption experiments. The overall sorp-
tion of o-xylene/p-xylene mixtures in cellulose tripropionate
(CTP) is given in fig. 4. As was already concluded from the swel-
ling experiments of the pure substances the affinity of CTP to
o-xylene is larger than to p-xylene.
In order to estimate the composition of a binary liquid mixture in
a membrane Krewinghaus [6] assumed a linear relationship between
the concentration of a component in the membrane and the concen-
tration outside the membrane (in the liquid feed mixture) accord-
ing to

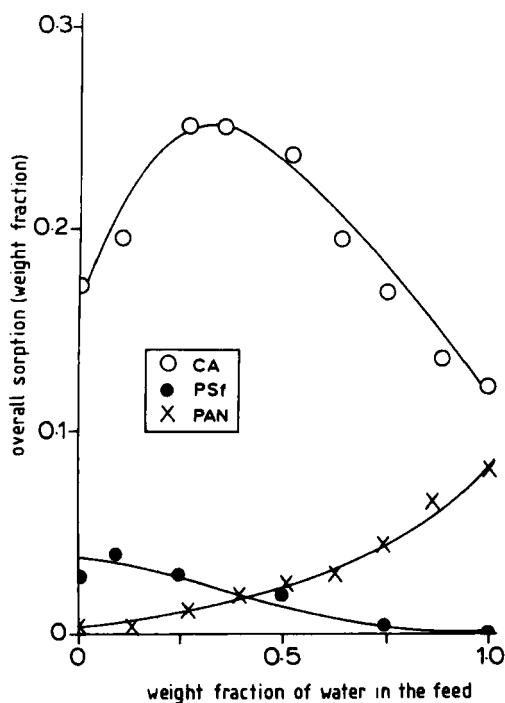$$c_i = x_i c_i^{\,o} \qquad\qquad\qquad [9]$$

FIGURE 3. TOTAL SORPTION AS A FUNCTION OF WATER CONTENT IN
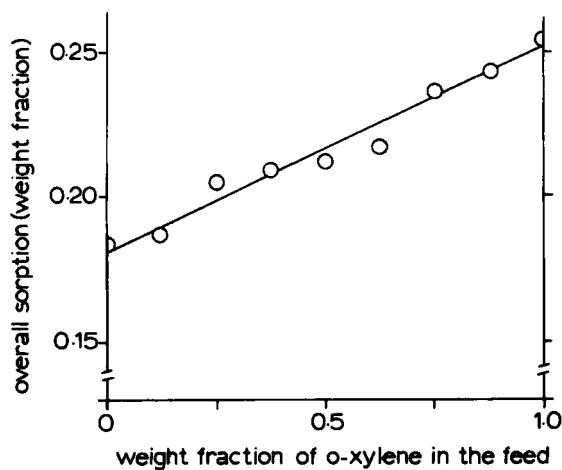WATER-ETHANOL LIQUID FEED MIXTURE FOR VARIOUS POLYMERS.

FIGURE 4. TOTAL SORPTION OF O-XYLENE/P-XYLENE IN CELLULOSE
TRIPROPIONATE AS A FUNCTION OF THE O-XYLENE
CONCENTRATION IN THE FEED.

where c_i is the concentration of component i in the membrane, x_i
is the mole fraction of component i in the liquid feed mixture and
$c_i{}^o$ is the solubility of the pure component in the membrane. When
eqn. [9] is applied to the results given in figs. 3 and 4 then it
can be deduced that for the system water/ethanol/CA, ethanol will
be sorbed preferentially over a major part of the composition
range, for the system water/ethanol/PAN, water will be sorbed
preferentially almost over the entire composition range and for
the system o-xylene/p-xylene/CTP, o-xylene will be sorbed prefe-
rentially for o-xylene concentrations in the feed larger than 50%
by weight.

Preferential sorption versus preferential permeation.

We have now come to the main issue of this paper, the relation
between preferential sorption and selective transport.
Fig. 5 gives the preferential sorption and pervaporation results
of the system water/ethanol/CA as a function of the weight
fraction of water in the feed.
It is obvious that both curves show the same behaviour. Water is
sorbed preferentially over the entire composition range and in the
pervaporation experiments a permselectivity is found for water
also over the entire composition range.
The preferential sorption and pervaporation results of the system
water/ethanol/PAN are given in fig. 6.
Again both curves show the same behaviour i.e. the component that
is sorbed preferentially also permeates preferentially.
Polyacrylonitrile shows, compared to cellulose acetate, very high
selectivities to ethanol-water mixtures.
Also for other systems it can be shown that preferential sorption
is the determining factor in selective transport. Fig. 7 gives the
preferential sorption and pervaporation results of the system
o-xylene/p-xylene/CTP. Again it is striking that both curves show
a similar behaviour. The component that is sorbed preferentially
(p-xylene) permeates preferentially too.

FIGURE 5.   EXPERIMENTAL VALUES FOR PREFERENTIAL SORPTION AND
            PERVAPORATION FOR THE SYSTEM WATER/ETHANOL/CELLULOSE
            ACETATE AS A FUNCTION OF THE CONCENTRATION OF WATER IN
            THE FEED

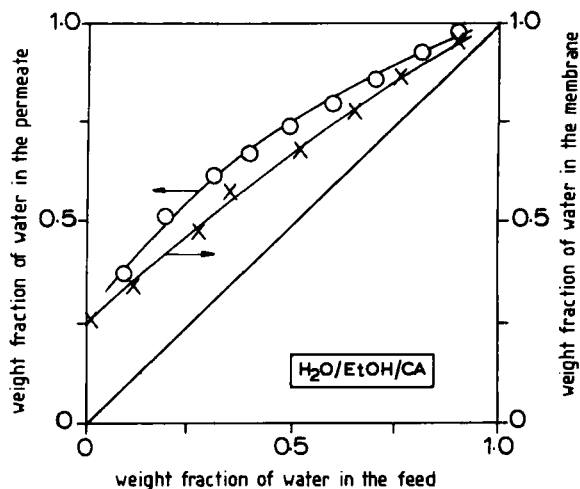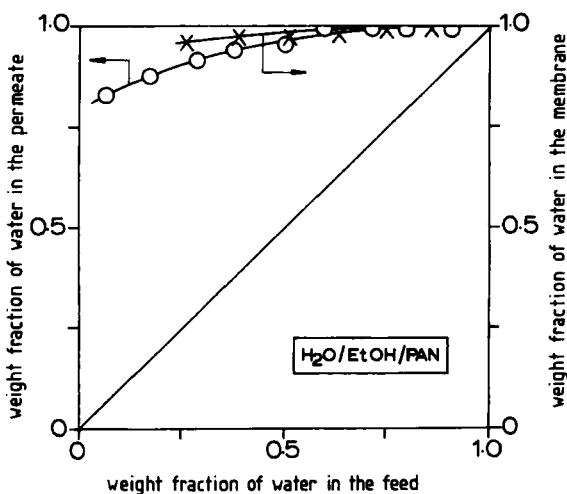

FIGURE 6.   EXPERIMENTAL VALUES FOR PREFERENTIAL SORPTION AND
            PERVAPORATION FOR THE SYSTEM
            WATER/ETHANOL/POLYACRYLONITRILE AS A FUNCTION OF THE
            CONCENTRATION OF WATER IN THE FEED.
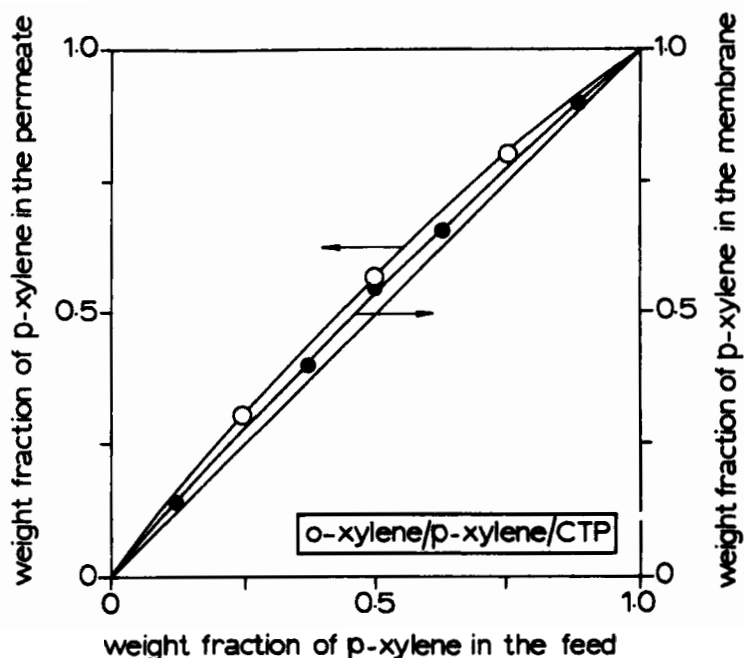
FIGURE 7.   EXPERIMENTAL VALUES FOR PREFERENTIAL SORPTION AND
            PERVAPORATION FOR THE SYSTEM O-XYLENE/P-XYLENE/CELLULOSE
            TRIPROPIONATE AS A FUNCTION OF THE CONCENTRATION OF
            P-XYLENE IN THE FEED.

Except for the systems described here there are a number of
literature sources showing evidently that preferential sorption is
the leading factor to selective transport. An overview of these
literature sources is given in table 4.

For all the systems given in table 4 it was demonstrated that the
component that is sorbed preferentially also permeates preferen-
tially. Especially the results of the system ethanol/1,2-dichloro-
ethane/PTFE-PVP are very striking [9] because an inverse in sorp-
tion selectivity results in an inverse in selective transport.

If these results are considered in terms of the solution-diffusion
model where the flux of a component is a function of solubility

TABLE IV

feed mixture	type of membrane	ref.
water/ethanol	cellulose acetate	11
water/ethanol	polyacrylonitrile	11
water/ethanol	polysulfone	11
water/ethanol	polymethylmethacrylate	30
p-xylene/o-xylene	cellulose tripropionate	12
ethanol/1,2-dichloroethane	PTFE-PVP	9
ethanol/chloroform	PTFE-PVP	9
acetic acid/1,2-dichloroethane	PTFE-PVP	9
benzene/cyclohexane	poly(γ-methyl-L-glutamate)	25
water/methanol	poly(γ-methyl-L-glutamate)	25
benzene/n-heptane	poly(butadiene-acrylonitrile)	26

(S) and diffusivity (D), this implies that the solubility part (or the ratio S_i/S_j) determines selective transport.

$$\alpha - \frac{J_i}{J_j} = f\left[\left(\frac{S_i(C_i,C_j)}{S_j(C_i,C_j)}\right),\left(\frac{D_i(C_i,C_j)}{D_j(C_i,C_j)}\right)\right] \qquad [10]$$

This does not mean that diffusivity is not important at all. The extent of permselectivity can also strongly be influenced by the ratio in diffusivities. Because multicomponent transport through (homogenous) membranes occurs generally in a coupled way the ratio of the diffusivities is difficult to estimate on forehand. For instance, if the results of the system water/ethanol/cellulose acetate are considered one can observe that sorption selectivity and permeation selectivity are almost equal (see fig. 5).

However, if the system water/ethanol/polysulfone is considered
[11] a small preferential sorption for water can be observed while
extremely high selectivities are obtained. This means that the
effective water diffusivity in polysulfone is much larger than the
ethanol diffusivity. Till now all the systems studied evidently
show that in selective transport the solubility ratio dominates
over the diffusivity ratio.
Another point to consider is that (preferential) sorption measure-
ments are equilibrium experiments while permeation experiments are
in fact non-equilibrium processes.

Discussion.

Transport in pervaporation takes place according to a solution-
diffusion model where both solubility and diffusivity affect se-
lective transport. From the investigations performed by us as well
as by others on the influence of preferential sorption on selec-
tive transport it has been proved experimentally that preferential
sorption is the factor that determines selective transport. This
was demonstrated for completely different mixtures and completely
different polymeric materials.
However the extent of selectivity can be influenced by differences
in diffusivities. Until now the occurrence of preferential sorp-
tion was often ignored or neglected and generally ideal sorption
was assumed i.e. the concentration of a component of a liquid
mixture inside the membrane was linearly related to the concentra-
tion of that component in the liquid feed mixture. There is enough
experimental evidence that this approach leads to incorrect results
even for systems from which it is assumed that they behave ideal-
ly. For instance for the system o-xylene/p-xylene/cellulose tri-
propionate, a weakly interacting system, p-xylene will be sorbed
over o-xylene over the entire composition ratio; when assuming
ideal sorption o-xylene would be the component that is sorbed

preferentially at high o-xylene concentrations in the feed. There-
fore preferential sorption measurements are preferred over overall
sorption measurements or pure component sorption measurements.
For a binary system consisting of polymer and penetrant (or perme-
ant) the affinity can be described adequately by the solubility
parameter theory in the case of hydrophobic substances while the
Flory-Huggins theory can be used for polar substances too. The
interaction parameters involved in these theories, δ-parameter and
χ-parameter respectively, are binary parameters. In general we are
interested in ternary systems consisting of a liquid feed mixture
and a polymeric membrane. Because in this case coupling phenomena
occur, even for weakly interacting systems, affinity or solubility
in a ternary system cannot be described or predicted anymore
neither by δ-parameters nor by χ-parameters only as was already
shown in the experimental section. It is possible to modify the
Flory-Huggins theory in such a way that ternary effects are taken
into account. There are several approaches to correct for ternary
effects. Pouchly [27,28] introduced a ternary interaction param-
eter χ_T. Another approach is to use concentration dependent inter-
action parameters [11,29]. In this way a better agreement can be
obtained between experiment and theory.

REFERENCES.

1. R.C. Binning et al.: U.S. Patents 2.923.749 (1960), 2.923.751
   (1960),2.953.502 (1960), 2.956.070 (1960), 2.958.657 (1960),
   2.970.106 (1961), 2.981.680 (1961), 2.985.588 (1961), 3.035.060
   (1962)
2. R.C. Binning, R.J. Lee, J.F. Jennings and A.C. Martin, Ind.
   Eng. Chem., 53, 45 (1961).
3. D.R. Paul and J.D. Paciotti, J. Pol. Sci. A-2, 13, 1201
   (1975).
4. C.H. Lee, J. Appl. Pol. Sci., 19, 83 (1975).

5. M.H.V. Mulder and C.A. Smolders, J. Membr. Sci., 17, 289
   (1984).

6. A.B. Krewinghaus, PhD Thesis, MIT Massachusetts, April 1966.

7. F.W. Greenlaw, R.A. Shelden and E.V. Thompson, J. Membr. Sci.,
   2, 333 (1977).

8. R. Rautenbach and R. Albrecht, J. Membr. Sci., 7, 203 (1980).

9. P. Aptel, J. Cuny, J. Jozefowicz, J. Neel and B. Chaufer, Eur.
   Pol. J., 14, 595 (1978).

10. F. Suzuki and K. Onozato, J. Appl. Pol. Sci., 27, 4229 (1982).

11. M.H.V. Mulder, A.C.M. Franken and C.A. Smolders, J. Membr.
    Sci., 22, 155 (1985).

12. M.H.V. Mulder, A.C.M. Franken and C.A. Smolders, J. Membr.
    Sci., 23, 41 (1985).

13. J. Pouchly and A. Zivny, Makromol. Chem., 183, 3019 (1982).

14. J.H. Hildebrand and R.L. Scott, "The solubility of
    non-electrolytes", Plenum Press, NY, 1949.

15. P.J. Flory, "Principles of Polymer Chemistry", Cornell
    University Press, Ithca, NY, 1953.

16. P.J. Flory, J. Am. Chem. Soc., 87, 1833 (1965).

17. I.C. Sanchez and R.H. Lacombe, Macromolecules, 11, 45 (1978).

18. E.B. Bagley and J.M. Scigliano, In 'Solutions and
    Solubilities', Ed. Dack, Chapter 3

19. I.C. Sanchez, in 'Polymer Blends', Vol. 1, Eds. D.R. Paul and
    S. Newman, Academic Press, NY 1982, p. 115

20. R.S. Chahal, W.P. Kao and D. Patterson, J. Chem. Soc. Far.
    Trans. 1, 10, 1834 (1973).

21. C.M. Hansen and K. Skaarup, J. Paint. Techn., 39, 511 (1967).

22. P.E. Froehling, D.M. Koenhen, A. Bantjes and C.A. Smolders,
    Polymer, 17, 835 (1976).

23. L. Broens, D.M. Koenhen and C.A. Smolders, Desalination 22,
    205 (1977).

24. M.H.V. Mulder, F. Kruitz and C.A. Smolders, J. Membr. Sci., 11,
    349 (1982).

25. F. Suzuki and K. Onozato, J. Appl. Pol. Sci., 28, 1949 (1983).

26. C. Larchet, J.P. Brun and M. Guillou, J. Membr. Sci., 15, 81 (1983).

27. A. Zivny and J. Pouchly, J. Pol. Sci. A-2, 10, 1467 (1972).

28. J. Pouchly and A. Zivny, Makromol. Chem., 183, 3019 (1982).

29. F.W. Altena, PhD-thesis, Twente University of Technology, 1982

30. T. Itoh, H. Toya, K. Ishihara and I. Shinohara, J. Appl. Pol. Sci., 30, 179 (1985).